

# Monitoring UT1 using VLBI and GPS estimates

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# Outline

1 – Combinations of astro-geodetic technique for Earth Rotation  
Status of the art

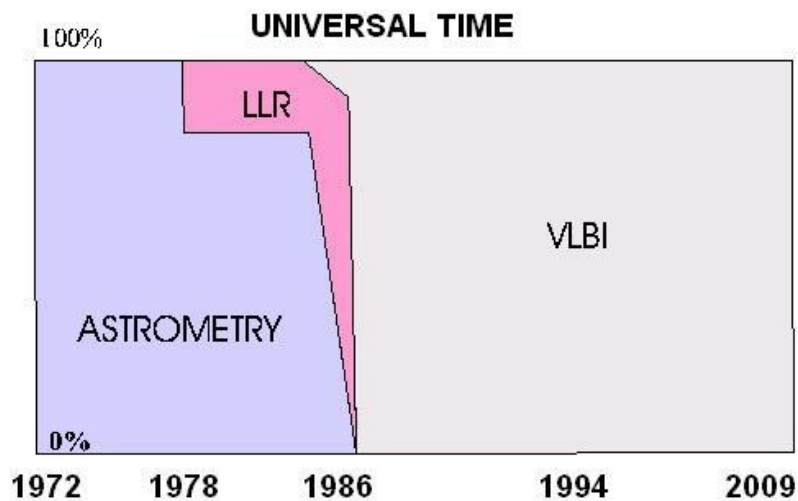
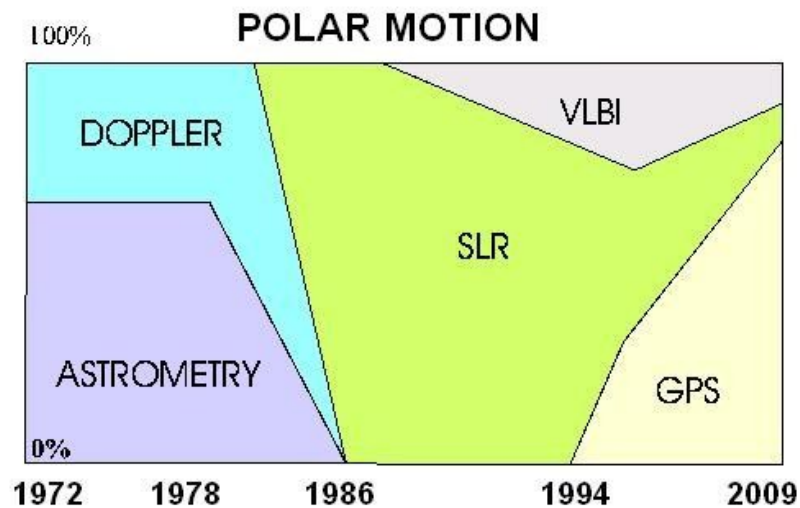
2 – What is the contribution of VLBI to IERS EOP ?  
Statistics, analyses and comparisons of different ACs series  
R1, R4, INT1, INT2

3 – Use of LOD GPS in UT1 estimation

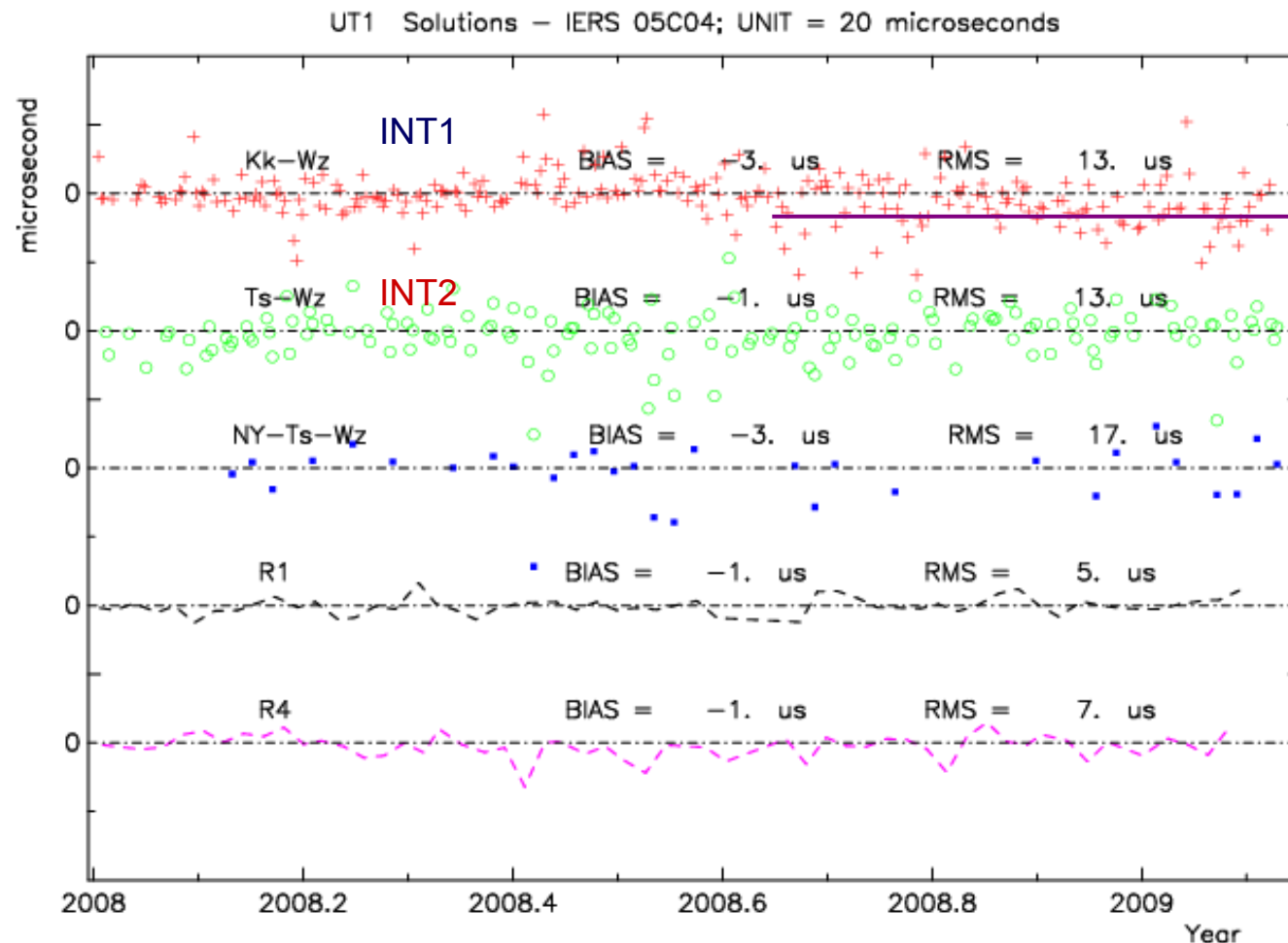
# Techniques contributing to IERS, evolution with time

<i>Technique</i>	<i>since</i>	<i>EOP</i>	<i>Time Res.</i>	<i>Present accuracy</i>	
<i>ASTROMETRY</i>	1899	Pole UT1 Nutation	5 days “ “	Pole: UT1: Nutation:	20 mas 1 ms 40 mas
<i>DOPPLER</i>	1972	Pole	2 days	Pole:	4 mas
<i>LLR</i>	1969	UT0	1 day	UT0:	0.1 ms
<i>SLR</i>	1976	Pole LOD	3 days “	Pole: LOD:	200 $\mu$ as 200 $\mu$ s
<i>VLBI</i>	1981	Pole Nutation UT1	3 days “ sub-daily - 1 day	Pole: Nutation: UT1:	100 $\mu$ as 60 $\mu$ as 5 $\mu$ s
<i>GPS</i>	1993	Pole LOD	sub-daily “	Pole: LOD:	30 $\mu$ as 8 $\mu$ s
<i>DORIS</i>	1995	Pole	3 days	Pole:	1 mas

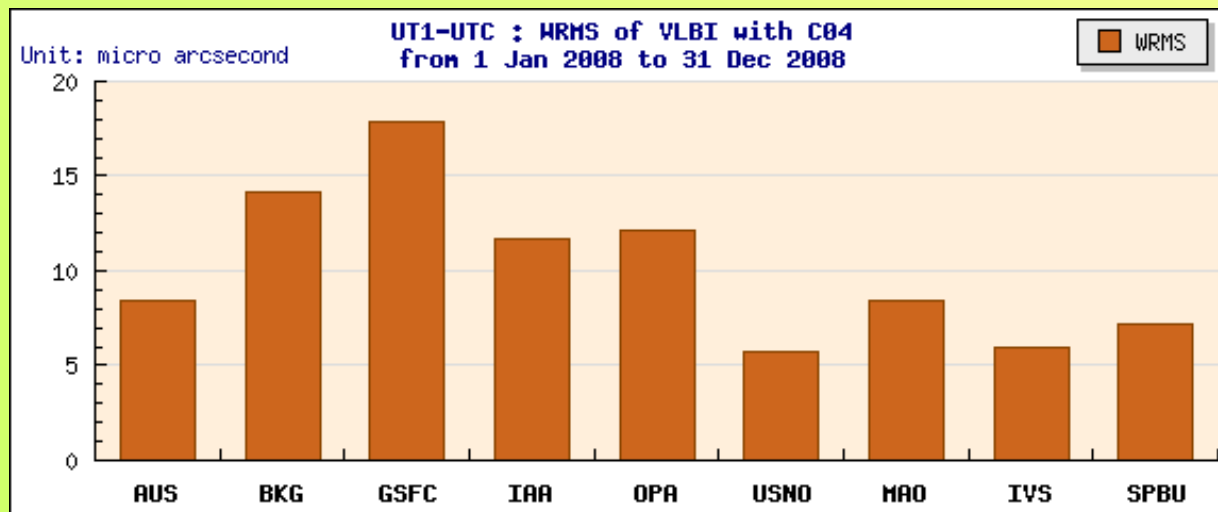
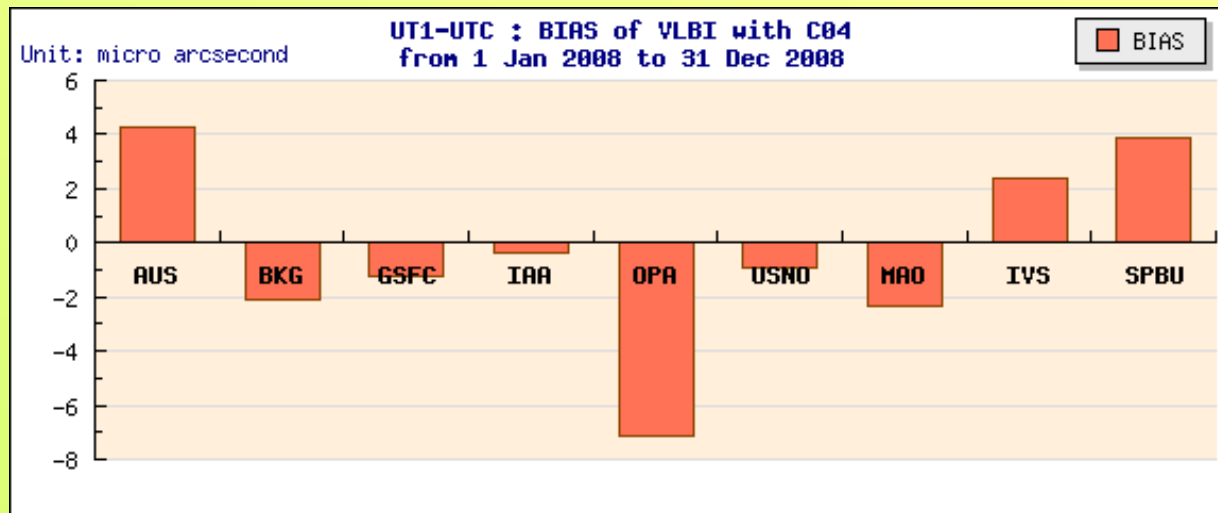
## CONTRIBUTION OF THE TECHNIQUES TO THE IERS COMBINED SOLUTIONS



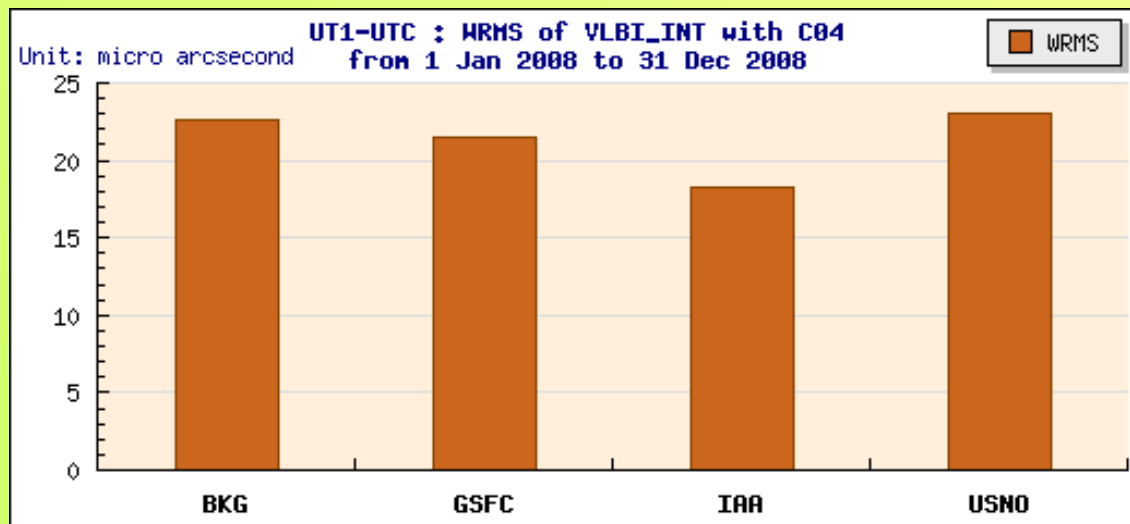
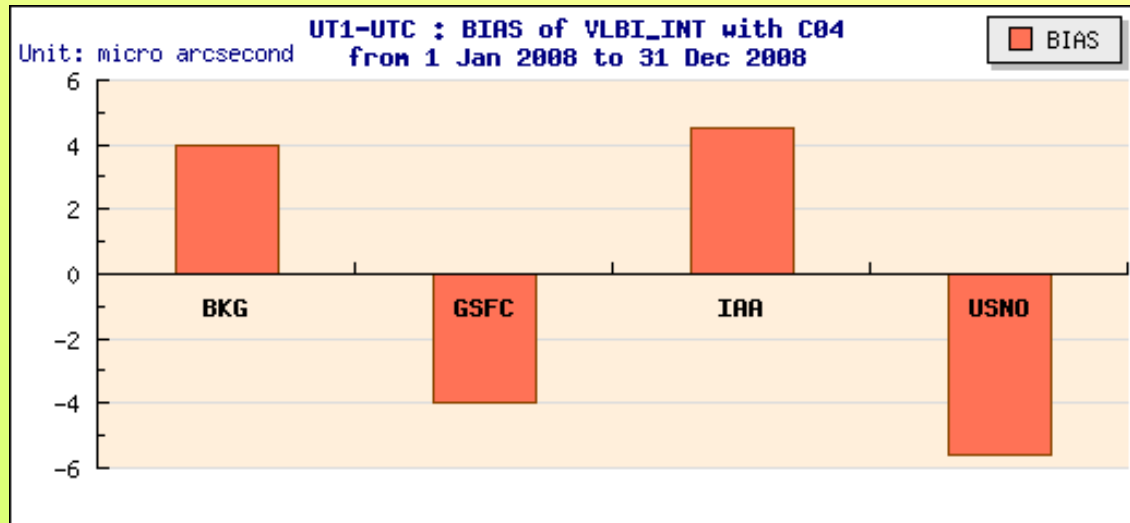
# Comparisons INT1, INT2 , R1 and R4 to C04



# VLBI standard, UT1



# VLBI intensive, UT1



# USE of LOD(GPS) for UT1



# Data

- UT1 standard VLBI sessions
  - Series from VLBI ACs (AUSLIG, GSFC, IAA, USNO, OPA, IAA, SPBU), GSFC R1 and R4
- UT1 , intensive sessions
- Daily LOD from IGS (igs00p03),  
12h epochs,  
Problem of systematic biases due to GPS orbit mis-modeling
- Integration of LOD can be used  
Densification  
Correct when VLBI intensive are erroneous (50-100  $\mu$ s possible)  
Fill gaps when UT1 intensive are missing (sometimes 4-5 days)  
Quasi-real time estimates (last VLBI intensive epoch to now)

# Method of Combined smoothing

- UT1 is observed by VLBI with a high long-term accuracy stability, with not high resolution (3/4 days), 5-8  $\mu\text{s}$
- UT1 intensive 15-20  $\mu\text{s}$
- LOD is observed by satellite methods with a short-term accuracy (10  $\mu\text{s}$ ) and high resolution (1 day)
- LOD first derivative of UT1  $\text{LOD} = -d(\text{UT1-TAI})/dt$

# Method of Combined smoothing

- Two relatively smooth curves
  - a) One fitting well to VLBI UT1 estimates
  - b) Second one fitting well to GPS LOD estimates
  - Both curves tied by constraints: latter is the first derivative of the former
- Combined smoothing is a generalization of Vondrak's smoothing (Vondrak and Gambis, 1999; Vondrak and Cepek, 2000)

Compromise between 3 conditions:

we define the values:

$$1. \quad S = \frac{1}{x_n - x_1} \int_{x_1}^{x_n} [\varphi'''(x)]^2 dt$$

'smoothness' of the first curve, where  $\varphi$  is estimated from Lagrange polynomial fitted to four consecutive points on the smoothed curve;

$$2. \quad F = \frac{1}{n-3} \sum_1^n p_i (\overset{\text{observed}}{y'_i} - \overset{\text{smoothed}}{y_i})^2$$

'fidelity' of the first curve to the observed values;

$$3. \quad \bar{F} = \frac{1}{n-3} \sum_1^n \bar{p}_j (\overset{\text{observed}}{\bar{y}'_j} - \overset{\text{smoothed}}{\bar{y}_j})^2$$

'fidelity' of the second curve to the observed first derivatives;

and we express the values  $\bar{y}_j$  in terms of  $y_i$  (from the first derivatives of the same Lagrange polynomial defining smoothness  $S$  above)

⇒ constraints assuring that the second curve is the time derivative of the first one, of the general form

$$\bar{y}_j = \sum_{i=1}^n a_i y_i$$



We are looking for the 'smoothed' function values  $y_i$  and the first derivatives  $\bar{y}_j$  as a (weighted) compromise among three conditions:

- a) the curve should be smooth (minimizing  $S$ );
- b) the values  $y_i$  should be close to the observed values of the function (minimizing  $F$ );
- c) the values  $\bar{y}_j$  should be close to the observed values of the first derivative (minimizing  $\bar{F}$ );
- d) the values  $y_i, \bar{y}_j$  are tied by the constraints above.

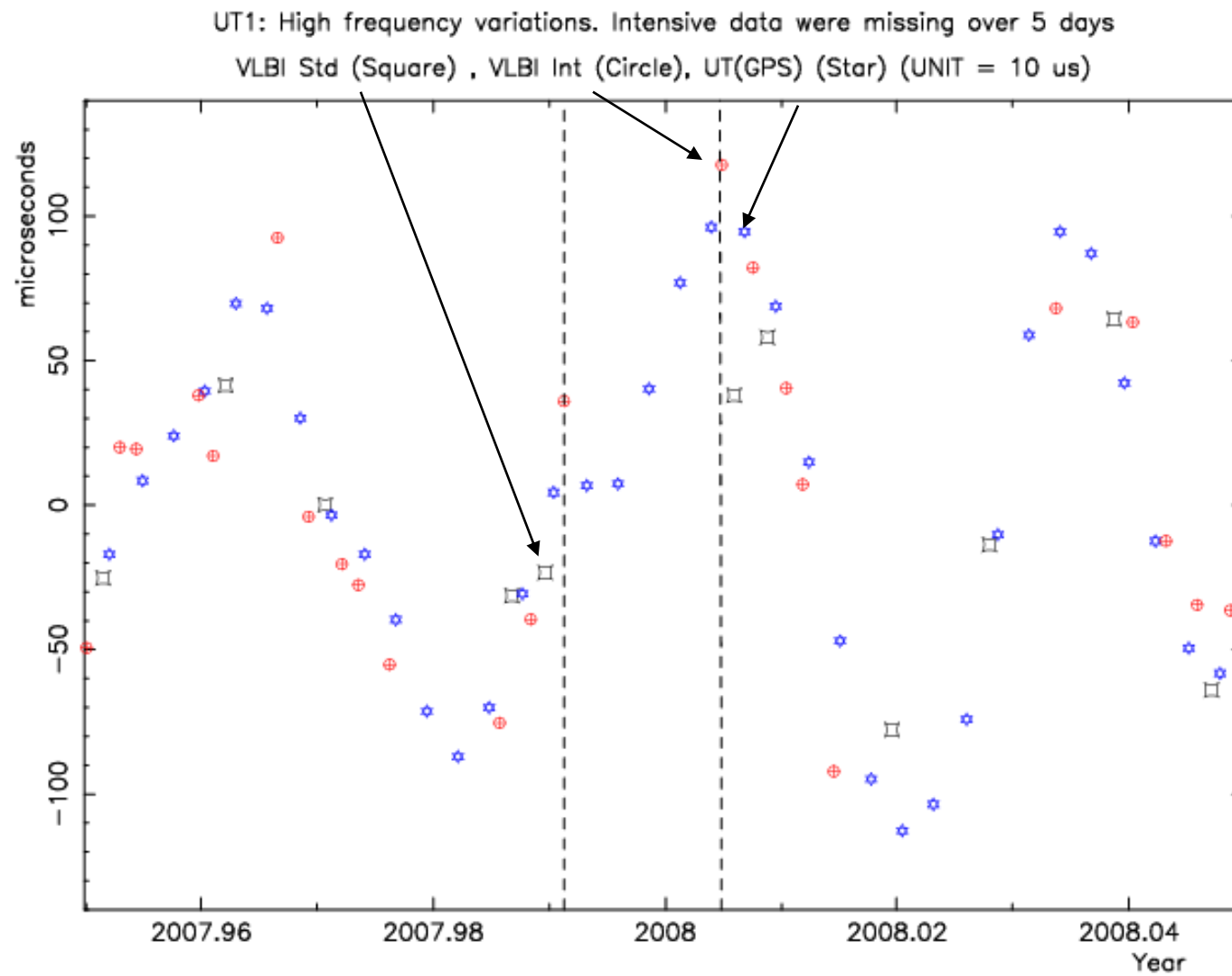
⇒ Adjustment by minimizing the expression

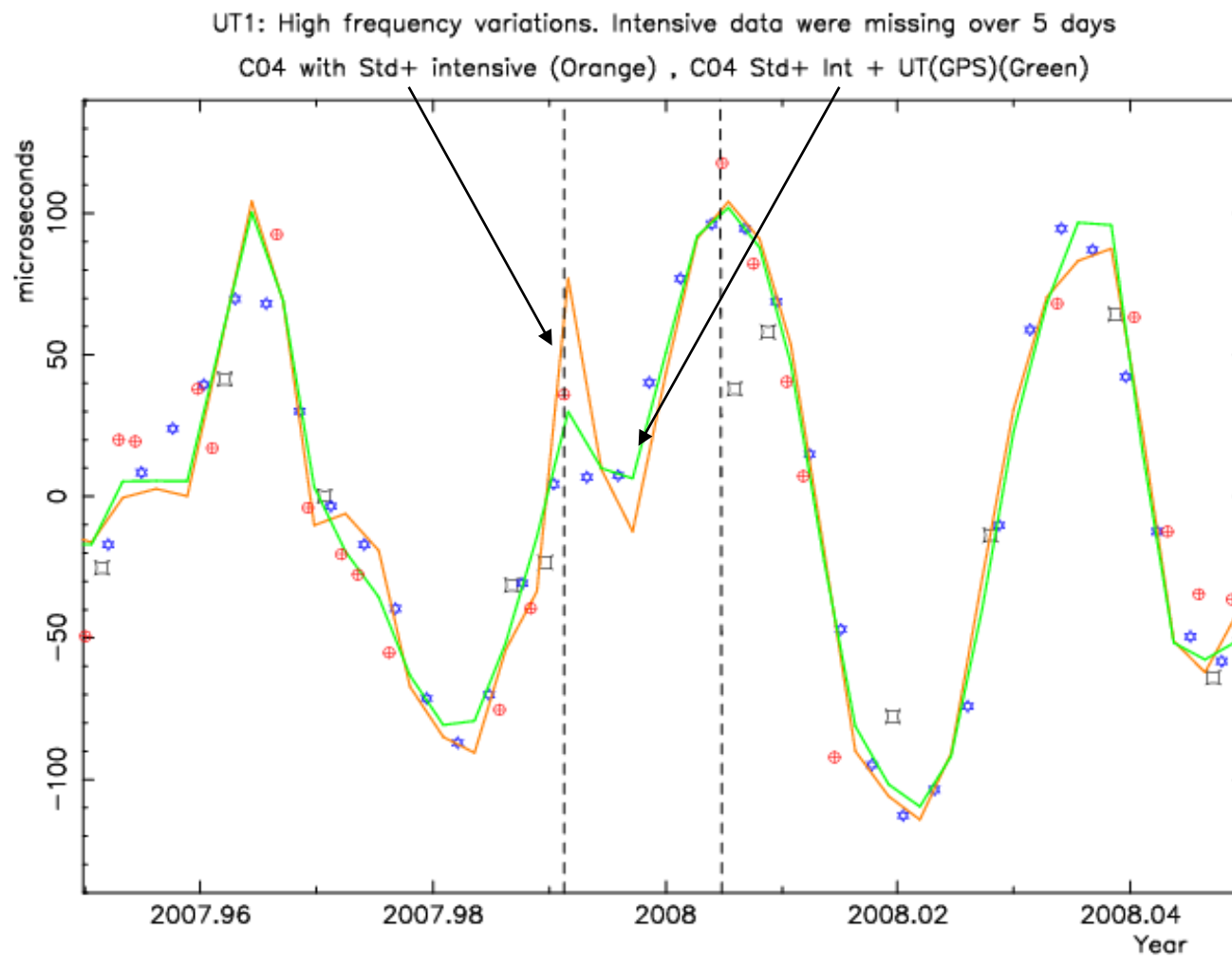
$$Q = S + \varepsilon F + \bar{\varepsilon} \bar{F} = \min.$$

$$\Rightarrow \frac{\partial Q}{\partial y_i} = 0$$

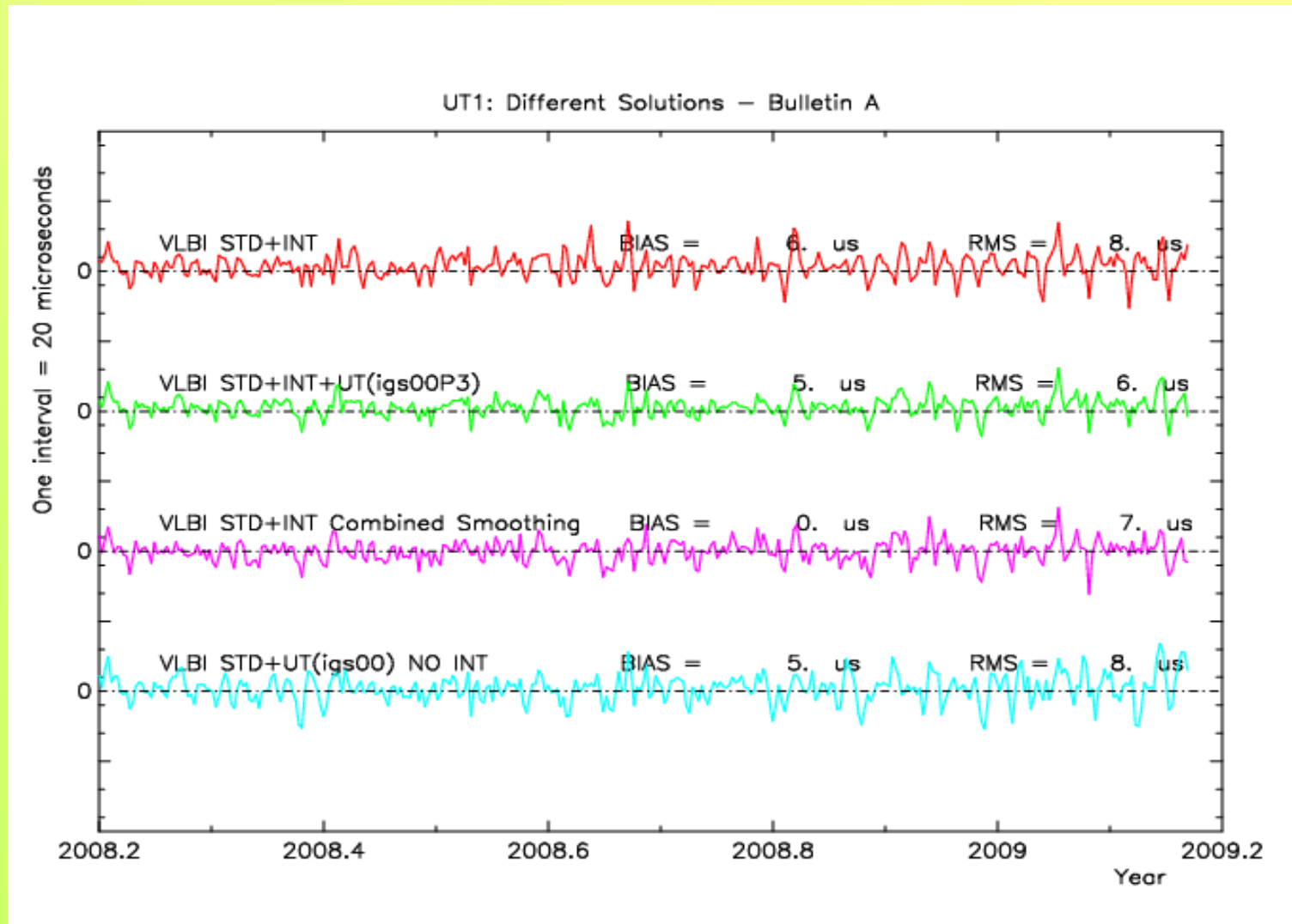
leading to the system of  $n$  linear equations (whose matrix is symmetric, with only 7 non-zero diagonals) for the unknowns  $y_i$ ; the values  $\bar{y}_j$  can be then easily calculated from the constraints.







# Comparison of various UT1 series to BULLETIN A





# CONCLUSIONS

- Current accuracy in the range of 5  $\mu\text{s}$  for Standard, 15-20  $\mu\text{s}$  for Intensive
- However, in case of erroneous data or gaps, UT(GPS) can be valuable to densify and homogenize UT1 estimates
- Combined smoothing using LOD(GPS) allows to improve the combination of UT1 and LOD
- Consistency of UT1 and LOD
- UT1: Gain of only 3  $\mu\text{s}$  (45  $\mu\text{as}$ ) when using intensive!!